SQUID

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Modern rock- and paleo-magnetism have come to strongly rely on extremely sensitive measurements provided by the superconducting quantum interference device (SQUID). At the IRM, both of our 2G magnetometers and both Magnetic Properties Measurement Systems (MPMS) operate using SQUIDs. Despite its pervasiveness in magnetometer systems of various sizes and shapes, a general understanding of how SQUIDs work is not widespread. For many people (including the author), the ten-armed variety (Fig. 1) is far more familiar and comprehensible (not to mention tasty). This short article aims to shine a little light on the subject. (Or, if you prefer, slather on a little garlic-butter sauce to make it more palatable.) Several excellent reviews of SQUID devices have been provided by others (Gallop and Petley, 1976; Goree and Fuller, 1976; Petley, 1980; Clarke, 1994), and the more rigorous mathematical details are left to them. Neither is this piece intended as a detailed description of electronics. Hopefully what will be provided is simply a little deeper understanding of what is going on when you hit that “measure” button on your instrument.

We will start with a review of the theoretical underpinnings of SQUID devices, and then move to descriptions of both the DC and RF SQUID and how they are operated as flux measurement devices.

The Theory

We begin our journey toward SQUID comprehension by starting with the basics, the SQU in SQUID: superconductivity and the quantization of magnetic flux.

Superconductivity. Certain metals when cooled below a critical temperature ($T_c$) are able to conduct current with zero resistance or voltage, an observation that earned the Nobel Prize for Dutch physicist Heike Kamerlingh Onnes in 1911. It wasn’t until 1957, however, with the description of BSC theory (Bardeen, Cooper, and Schrieffer, 1957) and the so-called Cooper pair, that the phenomenon was understood. In normal material, resistivity results from the interaction of electrons with the crystal lattice. In superconducting materials at $T < T_c$, lattice vibrations are suppressed and two electrons of opposite spin and momentum are weakly bound together as a Cooper pair and move through the lattice with zero resistance. In addition to a critical temperature, there also exist a critical field ($B_c$) and a critical current ($I_c$) above which a superconductor reverts to the normal state and develops resistance. The critical current is an important feature of the SQUID, as we will see below.

Flux quantization. In a closed loop of superconducting material, the flux threading the loop can only take on discrete values. This can be understood by considering that within a superconductor all the electrons (Cooper pairs) have the same quantum wave function, and around any closed path the phase ($\theta$) of this function must be an integral number such that $\oint d\theta = n2\pi$ (e.g. Gallop and Petley, 1976; Kleiner and Koelle, 2004). If the phase were to vary by a fraction of $n2\pi$, then the wave function would not be unique. In terms of angular momentum, all the Cooper pairs have the same angular momentum, which can only take on a discrete set of states according to the Bohr quantization rule (e.g. Rohlf, 1994; Goree and Fuller, 1976).

The total flux threading the loop is $\Phi = nh/2e$. (Eq. 2)

Figure 1. Chiroteuthis veranyi, by Georg Pfeffer, Die Cephalopoden der Plankton-Expedition, 1912.
Some tests to characterize a magnetic transition <40K in claystones

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Pyrrhotite (Fe₇S₈), siderite (FeCO₃) and rhodochrocite (MnCO₃) have a magnetic transition at 35K, 38K and 32K respectively [1-5]. This narrow range of temperature can lead to misinterpretations and our aim, during our 10-day visit, was to perform additional tests, including RT-SIRM, ZFC, K, hysteresis loops and FORC, to better understand the <40K magnetic transitions observed commonly in claystones.

Monoclinic pyrrhotite has a ~35K crystallographic transition of unknown origin [2, 6]. For pyrrhotite minerals >1 μm, this transition is characterized by a drop of RT-SIRM and LT-SIRM [6]. Siderite and rhodochrocite have Néel magnetic transitions from a paramagnetic to antiferromagnetic state [4, 5]. In rocks, there is generally a substitution between Mn²⁺ and Fe²⁺, resulting in a Néel temperature varying between 38K (siderite) and 32K (rhodochrocite) [5]. In siderite-bearing rocks, Housen et al. [3] observed a shift along the Y-axis of hysteresis loops for T<40K after applying a field-cooled (FC hysteresis loop). Kosterov et al. [5] observed similar shifts for rhodochrocite minerals (+Y or -Y) when measuring FC hysteresis loops measured below the Néel temperature (<40K).

Aubourg and Pozzi [7] observed a Néel-like magnetic transition at ~35K in claystones where pyrrhotite and magnetite constitute the magnetic assemblage. During the cooling of the RT-SIRM, an induced magnetization develops from ~80K parallel to the trapped magnetic field inside the MPMS [8]. Similarly, the warming of the LT-SIRM (obtained at 10K) showed a drop of one to two orders in magnitude from 10K to 50K, just like the pyrrhotite transition. Aubourg and Pozzi [8] proposed that this peculiar RT-SIRM transition, that they named the P-transition, is the signature of fine-grained pyrrhotite (< 1 μm).

We show representative results obtained from two claystones from Borneo prism. The samples S93 and S103 display similar ZFC curves (Fig. 1A) resulting in comparable derivative curves (Fig. 1A, inset). As Néel-like transition is sensitive to the trapped field inside the MPMS, which is variable from one instrument to another, we applied an upward magnetic field of 5μT during cooling of RT-SIRM (RT-SIRM is imparted at 300K with an upward magnetic field of 2.5T). The RT-SIRM curves on cooling show distinct patterns between the two samples (Fig. 1B). A P-transition is observed in sample S103. It is characterized by a regular increase of RT-SIRM from ~80K to 10K. In sample S93, we observe a sharp break-in-slope of the RT-SIRM at ~30K. The derivative curves of samples S93 and S103 precise these trends (inset, Fig. 1B). The P-transition behavior of sample S103 cannot be explained solely by the input of paramagnetic clays because the low-field magnetic susceptibility is similar for both claystones (K=62 μSΙ for sample S93 and K=87 μSΙ for sample S103).

We show FC hysteresis loops obtained from ~10K to ~100K after slope correction (Figure 2A). Both samples show strong paramagnetic input at room temperature (data are not shown). In sample S103, the hysteresis loops are well centered through the origin and the coercivity remains low (Fig. 2A). By contrast, for sample S93, a positive shift along the Y-axis is observed for 10K to 30K. Similarly, we note an increase of coercivity because saturation is not achieved at 1T at 10K. This +Y shift is diagnostic of siderite [3] and rhodochrocite [5]. When cooled below the Néel temperature, siderite and rhodochrocite get a strong coercive magnetization (Hc >> 1T) that is not erased when running hysteresis loops.

We ran also FORC diagrams obtained at 300K, 100K and 20K (results are not shown). At 300K, these strong paramagnetic claystones S103 and S93 display the signature of low-coercive magnetic mineral, likely magnetite which is consistent with the Verwey transition observed in ZFC and RT-SIRM curves (Fig. 1). At 100K, the paramagnetic input is lower and the FORC are more representative of the magnetic assemblage. In both claystones, we see an assemblage of non-interacting magnetic...
minerals in the range of coercivity from few mT up to 80 mT. This is consistent with an assemblage of magnetite and possibly pyrrhotite. At 20K, the FORC of S103 and S93 are different. The coercivity is soft for sample S103, while a stripe develops for sample S93, attesting for a distribution of a large coercivity spectrum.

We performed susceptibility measurements at different magnetic fields (from ~16 to ~240 A/m). We did not observe any field-dependency. However, the out-of-phase magnetic susceptibility (K') increases for both samples from ~40K to 5K (Fig. 3) Note that there is two orders of magnitude between K’ of S103 and K’ of S93. K’ is larger in sample S103 where P-transition develops. There are several ways to interpret the increase of K’. One is to consider that the mineral conductivity increases significantly and that Foucault currents developed. Besnus [9], who was the first to recognize the ~35 K transition in pyrrhotite crystals, observed a large drop of resistivity from ~50K and below. It was even believed that the pyrrhotite might be a superconductor for T<35K (G. Fillion, Institut Néel, pers. com., 2008).

From this set of low-temperature measurements, we propose that magnetite and rhodochrocite constitutes the main magnetic assemblage of claystones S93. In claystones S103 where magnetite is also present, we propose that the P-transition is due to the contribution of fine-grained (<1 μm) pyrrhotite although we cannot rule out completely the input of a rhodochrocite-like Néel transition.

To distinguish between rhodochrocite-like carriers and pyrrhotite-like carriers in claystones, the ZFC curves are not adapted (Fig. 1A). RT-SIRM can help by applying a weak magnetic field (5 μT) during cooling, leading to the identification of a P-transition (Fig. 1B). FC-hysteresis loops below the Néel temperature of siderite and rhodochrocite allows identifying shifted-loops along Y-axis, which are diagnostic of siderite and rhodochrocite (Fig. 2). The identification of a sharp increase of the out-of-phase magnetic susceptibility from ~40K is diagnostic of claystones which display the P-transition (Fig. 3) and thus possibly the occurrence of ultra fine pyrrhotites.

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References

Figure 3: Out-of-phase magnetic susceptibility of samples S93 and S103. Note that the scale is two-order larger in magnitude for sample S93.

Contribution of biogenic minerals found in ants and termites to the magnetic properties of soils

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Biomineralization by social insects has been described in literature for more than two decades [1-5]. The presence of magnetite particles in migratory ants (Pachycondyla marginata) occurring in southeastern Brazil was reported by Acosta-Avalos et al. [6]. These ants seem to follow an approximately north-south direction during migration [7], and they prey on live termites of the species Neocapritermes opacus, in which Esquivel et al. [4] and Oliveira et al. [5] also identified magnetic particles. Starting from the premise that the magnetic particles produced by these insects are released in the environment, and contribute to the magnetization of the soil, we are conducting a comparative magnetic characterization of the soil and the insects.

Soil samples were collected from two sites (samples 40 and 41) at 5m and 10m from the ant nest. At each site samples were taken at the surface and at depths of 25cm and 45cm (samples labeled a, b, and c, respectively). Two other samples (42 and 43) were collected from the termite and ant nests, respectively.

The magnetic measurements consisted of hysteresis loops (high and low-temperature), ZFC/FC curves and RTSIRM performed during my stay at IRM from 2-12
September, 2008. Hysteresis loops were performed at room and low-temperature for 13 samples of soil and for the insects. Maximum field of 1.5 T was applied at select temperatures from \( \approx 10 \) K to 300 K, and measurements were made by means of a vibrating sample magnetometer (VSM) with a liquid He cryostat. Room temperature loops for the termite nest and soil samples (Figure 1) show very similar behavior. These results as well as the coercive force variation with temperature point to the presence of titanomagnetites \([8, 9]\) as in a pseudo-single domain scale as shown by the Day plot \([10]\).

Low-temperature remanence measurements were made from 10 K to 300 K with a Quantum Design (MPMS2) SQUID magnetometer. Samples were cooled down to 10 K in zero field, and measurements were made up to 300 K at steps of 10 K. The ZFC/FC and RTSIRM remanence curves for the termite nest sample show very similar pattern (Fig. 2A, 2C) with no Verwey transition characteristic of magnetite. The ant nest show a similar behavior (Fig. 2B, 2D). However, low temperature remanence variation curves show slight inflections between 100 K and 120 K, probably related to PSD titanomagnetite.

According to the above results all samples displayed similar behavior indicating that PSD titanomagnetite are found both in the termite nest and surrounding soil. No differences were noticed for soil samples from different depths. Results from termites (ZFC/FC, RTSIRM and hysteresis loops) are very similar to the nest and soil sample (Fig. 2E, 2G), but ants seem to display magnetic characteristics comparable with magnetite (Verwey transition at 120K) (Fig. 2F, 2H). Further interpretations are still in progress.

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References

Current Articles

A list of current research articles dealing with various topics in the physics and chemistry of magnetism is a regular feature of the IRM Quarterly. Articles published in familiar geology and geophysics journals are included; special emphasis is given to current articles from physics, chemistry, and materials-science journals. Most abstracts are taken from INSPEC (@ Institution of Electrical Engineers), Geophysical Abstracts in Press (@ American Geophysical Union), and The Earth and Planetary Express (@ Elsevier Science Publishers, B.V.), after which they are subjected to Procrustean culling for this newsletter. An extensive reference list of articles (primarily about rock magnetism, the physics and chemistry of magnetism, and some paleomagnetism) is continually updated at the IRM. This list, with more than 10,000 references, is available free of charge. Your contributions both to the list and to the Abstracts section of the IRM Quarterly are always welcome.

Anisotropy


Archeomagnetism


Bio(geo)magnetism


Environmental Magnetism and Paleoclimate


Mineral and Rock Magnetism


Harrison, R.J., Magnetic ordering in the ilmenite-hematite solid


Mineral Physics and Chemistry


Tectonics/Paleomagnetism


Other


and the fundamental flux quantum is therefore
\[ \Phi_0 = \frac{h}{2e} \approx 2 \times 10^{-15} \text{Wb} \]  
\[ \text{Eq. 3} \]
where \( h \) is Planck’s constant (\( h/2\pi \)), \( e \) is the charge on an electron, and the factor of two accounts for the fact that the electrons travel in Cooper pairs.

To envision how flux quantization and superconductivity could allow us to measure magnetic fields, imagine a superconducting ring in the presence of a steadily increasing flux (Fig. 2). As the external flux (\( \Phi_E \)) increases, a persistent (super)current is induced in the loop. (Because current flows without resistance, it will persist until the external flux changes.) The current in turn induces a flux (\( \Phi_c \)) inside the loop that is equal and opposite to \( \Phi_E \). The total flux inside the loop (\( \Phi_i \)) remains constant (at zero \( \Phi_0 \)) and is the sum of the external flux and that generated by the current in the loop. When the critical current is reached (in this example at a flux of 0.75 \( \Phi_0 \)), the loop is no longer superconducting and a flux quantum can enter the loop. The quantum state of the loop has now changed by +1, and the total flux inside the loop is 1 \( \Phi_0 \). This requires the current to reverse direction so that \( \Phi_c + \Phi_i = 0.75 + 0.25 = 1 \Phi_0 \). As the external flux continues to increase, the current decreases (and then increases again in the opposite direction) so that the flux inside the loop remains at 1 \( \Phi_0 \). When \( I_c \) is again reached, the loop reverts to its normal state and another flux quantum enters. The step-wise nature of the flux increases in the ring makes them easy to count, and in theory, by monitoring the current and the number of times it makes discrete jumps, one could precisely measure both flux quanta and fractions of flux quanta.

In practice, the above-described flux switching device is not very sensitive. The size of the loop is constrained by thermal energy considerations to be so small that sensitivity would be very limited. Additionally, the field required to exceed the critical current is large enough that the device operates ineffectually (Goree and Fuller, 1976). A number of applications allow for more sensitive flux switching, and the Josephson junction is perhaps the most important.

The Josephson Effect and Josephson Junction.
Brian Josephson predicted in 1962 that supercurrent will flow between two superconductors separated by an insulator. Although the original Josephson junction consisted of an insulating layer separating two superconductors, similar behavior is observed with any kind of weak link between two superconductors. Other types of junctions include a thin oxide layer, a narrow constriction, a superconducting point contact, or a normal (non-superconducting) metal sandwich junction (Gallop and Petley, 1976; Petley, 1980). (See back cover for an example junction.)

We can understand this Josephson effect if we remember that all Cooper pairs in a superconductor have the same quantum-mechanical wave function. If the insulator is narrow enough, the waves on either side of the insulating junction overlap, allowing the Cooper pairs to “tunnel” through the insulator. The critical current across such a junction is much less than in a true superconductor, so that in a superconducting ring containing a Josephson junction, flux switching will occur at smaller applied field increments.

The current flowing across the junction is a function of the phase difference (\( \delta \)) between the two superconductors on either side of the insulator:
\[ I = I_c \sin(\delta), \]  
\[ \text{Eq. 4} \]
where \( I_c \) is the critical current of the junction. Equation 4 is known as the DC Josephson effect. There are many other fascinating phenomena associated with tunneling behavior and Josephson junctions in presence of current and magnetic flux, but in the interest of simplicity, we will rudely overlook them for now.

When a weak link or Josephson junction is inserted in a superconducting ring, the requirement that the total phase difference around the loop be \( 2\pi \) (Eq. 1) still holds and takes the form:
\[ \delta + 2\pi \frac{\Phi_c}{\Phi_0} = 2\pi n \]  
\[ \text{Eq. 5} \]
where \( 2\pi \Phi_c/\Phi_0 \) is the phase difference due to the flux threading the loop. It follows that flux threading a loop is no longer precisely quantized (Petley, 1980), i.e. \( \Phi_c/\Phi_0 \) can take on fractional values because of the phase difference across the junction.

Putting it all together
There are two ways in which the Josephson junction is typically used to measure magnetic flux: the single-junction (RF) SQUID and the double-junction (DC) SQUID.

Figure 2. In the presence of a steadily increasing external field (a), the current in a superconducting ring is generated (b), which in turn induces an equal and opposite flux (c). The total flux inside the loop is quantized (d). In this example, the critical current of the ring is reached at \( \Phi = 0.75\Phi_0 \).
The DC SQUID has considerably higher precision and was developed first, but for many years was not in common use because of the high cost of manufacturing the junctions. Now that junction fabrication is far less costly, most new instruments use the DC SQUID. Simplified descriptions of DC and RF SQUIDS are given below and draw heavily on Clarke (1993), Braginski and Clarke (2004), and Bruynseraede et al (1993).

**The Double Junction (DC) SQUID.** The DC SQUID consists of two identical Josephson junctions arranged in parallel on a superconducting loop (Fig. 3a). Each junction has a critical current $I_0$, and a DC bias current ($I_B$) is applied to the device. In the absence of any applied (external) flux (and for $I_B < 2I_0$), the current flowing across each junction is $I_B/2$. The critical current for the entire device ($I_C$) is $2I_0$, at which point both junctions revert to the normal state simultaneously. Additionally, the phase change across the entire device ($\delta$) should be independent of the path traveled and thus equal to the phase change across each junction: $\delta = \delta_1 = \delta_2$.

In the presence of increasing external (sample) flux ($\Phi$), a circulating current is induced in the ring ($I_\Phi$) to counter the applied flux. This current adds to the bias current in junction 1 ($I_1 = I_B/2 + I_\Phi$) and subtracts from the bias current in junction 2 ($I_2 = I_B/2 - I_\Phi$). Now, junction 1 will reach its critical current before junction 2 (when $I_B/2 + I_\Phi = I_0$); when this happens, the device reverts to the normal state, a flux quantum enters the ring, and the circulating current reverses direction (Fig. 3b). The limiting critical current for the entire device is therefore $I_C = 2I_0 - 2I_\Phi$ and varies periodically with applied flux (Fig. 3c) as the two junctions interfere with each other. This interference is analogous to that generated by optical waves in a double slit experiment; in this case a single quantum-mechanical wave is “split” by the junctions into two waves that interfere with each other so as to modulate the critical current of the device.

Slightly more formally, the total current across the device is the sum of the current across each junction: $I_B = I_1 + I_2$, and by Equation 4, the current across each junction is a function of the phase change across the junction:

$$I_C = I_0 \sin(\delta_1) + I_0 \sin(\delta_2)$$  \hspace{1cm} Eq. 6

In the absence of any flux, $\delta_1 = \delta_2 = \delta$ (above), and therefore $I_1 = I_2$. In the presence of flux threading the loop, the total phase change around the loop is given by Equation 5, and the phase change across each junction (in the direction of $I_B$) is:

$$\delta_1 = \delta + \pi \Phi_\text{T}/\Phi_0$$  \hspace{1cm} Eq. 7

$$\delta_2 = \delta - \pi \Phi_\text{T}/\Phi_0$$  \hspace{1cm} Eq. 8

The total current across the device is therefore:

$$I = I_0 \sin(\delta + \pi \Phi_\text{T}/\Phi_0) + I_0 \sin(\delta - \pi \Phi_\text{T}/\Phi_0)$$  \hspace{1cm} Eq. 9

or

$$I = 2I_0 \sin(\delta) \cos(\pi \Phi_\text{T}/\Phi_0)$$  \hspace{1cm} Eq. 10
The maximum supercurrent, or critical current, is achieved when \( \sin(\delta) = 1 \), so
\[
I_c = 2l_0 \cos \left( \frac{\pi \Phi_L}{\Phi_0} \right) \quad \text{Eq. 11}
\]

In practice, the DC SQUID is operated at a bias current that is greater than \( I_c \) (e.g. point D in Fig. 4a). In this mode, a voltage develops across the device (Fig. 4a) that is a function of both \( l_0 \) and \( \Phi_e \) (or \( \Phi_{\text{SAM}} \) when the external flux results from a sample approaching the SQUID). Voltage is at a maximum where \( I_c \) is minimized at \( (n+1/2)\Phi_0 \), and \( V \) is at a minimum where \( I_c \) is maximized at \( n\Phi_0 \). Because \( I_c \) varies with applied flux (Fig. 3c), at constant \( l_0 \) output voltage also varies periodically with the applied flux (Fig. 4b).

The Single Junction (RF) SQUID. The RF SQUID consists of a superconducting loop of inductance \( L \) containing a single junction. The operation of this device is more difficult to understand intuitively, but we start by noting that the RF SQUID is not technically a SQUID; with only one junction, it does not operate using the interference phenomenon described above for the DC SQUID. In the RF SQUID, the loop is inductively coupled to a resonant circuit\(^1\), which is driven at (or near) its resonant frequency by the current \( IRF \) (Fig. 5). A voltage across the resonant circuit provides the device output.

The current flowing across the junction (and around the ring) is easily derived from Equations 4 and 5 and is
\[
I_c = 2l_0 \sin(2\pi \Phi_e/\Phi_0)
\]
The resulting relationship between applied (external) flux \( \Phi_e \) and flux inside the ring \( \Phi_e \) is shown in Figure 6 (for the most commonly-used case where \( 2\pi L_1 \geq \Phi_0 \) ). The external flux is the sum of an alternating flux generated by the resonant circuit/RF coil \( \Phi_{\text{RF}} \), and a quasi-static flux from the sample being measured \( \Phi_{\text{SAM}} \).

For the moment, let us ignore the sample contribution and consider the operation of the device only in the presence of the RF field \( \Phi_e = \Phi_{\text{RF}} \). This function is represented by the thin gray dashed curve in Figure 6a. Only the positively sloping segments are stable, because when the alternating external flux is large enough to cause \( I_o > I_c \), flux will enter or exit the ring, and the device will trace out the path indicated by the heavy, solid (red) lines.

The peak output voltage \( V_{\text{RF, max}} \) measured across the resonant circuit is a function both of the RF drive current and of the sample flux (Fig. 6b). Let us continue to consider the case where \( \Phi_{\text{SAM}} = 0 \). For small values of \( l_{\text{RF}} \) not enough flux is generated to cause the SQUID to exceed its critical current, and it remains in the “zero” quantum state, tracing a path back and forth along a portion of line segment \( ae \) (Fig. 6a). Until \( l_{\text{RF}} \) reaches \( A \), \( V_{\text{RF, max}} \) increases linearly with \( l_{\text{RF}} \) (Fig. 6b). When the drive current reaches \( A \), the applied flux is sufficient to cause the SQUID to exceed \( I_c \), it temporarily admits a quantum of flux, and follows the path \( abc \) or \( efgh \) (Fig. 6a). This transition causes energy to dissipate in the resonant circuit, meaning that the peak induced flux on the next half-cycle will be less than that required to reach the \( ab \) or \( ef \) transition, even though \( l_{\text{RF}} \) remains at \( A \). The device will stay in the initial (quantum) state on path \( ae \), building up energy over

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\(^1\) A resonant circuit consists of a capacitor (C) connected to an inductor (L). Current can alternate between the two at the circuit’s resonant frequency. The circuit is also known as an LC circuit, or a tank circuit because the oscillating behavior of the current is similar to water sloshing back and forth in a tank.
the course of many RF cycles. Eventually, $\Phi_{\text{IRF}}$ will be sufficient to make the $ab$ or $ef$ transition again, and the process will be repeated. As $I_{\text{RF}}$ is increased beyond $A$, the quantum transitions ($ab$ or $ef$) still occur at the same voltage, but this peak voltage is achieved more frequently. When the drive current reaches point $B$, each cycle of the RF causes the SQUID to execute a complete double-hysteresis loop ($abedfgh$), and further increases in $I_{\text{RF}}$ now cause an increase in the measured peak voltage (Fig. 6b). At $I_{\text{RF}} = C$, there is sufficient flux to exceed $I_c$, twice, admitting two flux quanta ($ab$ and $ij$), and so on.

The relationship between $I_{\text{RF}}$ and $V_{\text{RFmax}}$ varies depending on the sample flux; for $\Phi_{\text{SAM}} = n\Phi_0$, the relationship is as shown by the solid (red) line. For $\Phi_{\text{SAM}} = (n + \frac{1}{2})\Phi_0$, the curves shown in Figure 5a are shifted by $\Phi_0/2$ (heavy, dashed blue line), and the transition to a higher flux state ($ab$) can occur at a lower drive current ($A'$). $I_{\text{RF}}$ is usually chosen to maximize the voltage change with change in $\Phi_{\text{SAM}}$, and the device is operated at this constant $I_{\text{RF}}$ (point $D$ in Fig. 6b). $V_{\text{RFmax}}$ then varies with applied field ($\Phi_{\text{SAM}}$), generating the output signal (Fig. 6c).

The relatively simple DC and RF devices described above become more complicated in actual operation. For example, because the SQUID itself is quite small (less than a few mm), it is typically inductively coupled to a larger-diameter superconducting pick-up coil, which provides a larger signal. Other efforts to increase the signal to noise ratio, practically measure the device output, account for hysteretic current-voltage behavior in the Josephson junctions, and many other considerations are beyond the scope of this short article. However, we will finish up by exploring one of these issues.

The Flux Locked Loop (FLL) and the Dreaded Flux Jump (DFJ). Because the applied flux to voltage relationships (Figs. 4b and 6c) are sinusoidal — especially for DC SQUIDs — the output response is non-linear for all but the smallest variations in $\Phi_E$. To resolve this problem, the SQUID is usually operated in a flux-locked loop (FLL), or at constant flux. A feedback loop applies a flux to the SQUID that is equal and opposite to that generated by a sample. This both linearizes the output signal, and greatly increases the dynamic range of the SQUID. The feedback range is generally set to $\pm 1\Phi_0$, and each time the range is exceeded, the feedback is reset to zero and a flux quantum is counted. In this way, there is both a digital and an analog part to the signal: the number of flux quanta counted and the voltage representation of a fraction of a flux quantum, respectively.

And so ends our whirlwind tour of SQUIDs. Hopefully the next time you use one, you will have a little better appreciation for what’s going on behind the curtain. And if you are still a little bit baffled, draw some comfort from Aslamazov and Varlamov (2001), who note in a discussion of SQUIDs, that “...superconductivity is a complicated quantum effect. Those who want really to comprehend it have a long and hard way ahead of them. It demands many years of resolute but rewarding work.” Or, if you don’t have that much time, come visit the IRM during the Minnesota State Fair, where you can surely get deep-fried SQUID on a stick — less useful, but perhaps more satisfying.

References:

Brian David Josephson
b. 4 January, 1940, Cardiff, Wales, United Kingdom

Brian Josephson started at Cambridge University as an undergraduate, where he published his first paper reconciling differing measurements of gravitational red shift by calculating a thermal correction to the Mossbauer effect. He continued his studies at Cambridge, receiving a Masters and then a Ph.D. in Physics in 1964. Josephson is probably best known for his theoretical work on tunnel barriers in superconductors. This work was largely carried out while a graduate student and won him the Nobel Prize in Physics in 1973, which he shared with Leo Esaki and Ivar Giaever. The Josephson junctions which grew out of this work allow modern SQUID magnetometers to operate with extremely high sensitivity. Josephson moved briefly to the United States to work as a Research Assistant Professor at the University of Illinois before returning to Cambridge in 1967 to serve as Assistant Research Director of the Cavendish Laboratory. Now retired as Professor of Physics and member of the Theory of Condensed Matter Group, Josephson continues working as Director of the Mind-Matter Unification Project at the Cavendish Laboratory.
The Institute for Rock Magnetism is dedicated to providing state-of-the-art facilities and technical expertise free of charge to any interested researcher who applies and is accepted as a Visiting Fellow. Short proposals are accepted semi-annually in spring and fall for work to be done in a 10-day period during the following half year. Shorter, less formal visits are arranged on an individual basis through the Facilities Manager.

The IRM staff consists of Subir Banerjee, Professor/Founding Director; Bruce Moskowitz, Professor/Director; Joshua Feinberg, Assistant Professor/Associate Director; Jim Marvin, Emeritus Scientist; Mike Jackson, Peat Solheid, and Julie Bowles, Staff Scientists.

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Right: Example of a Josephson junction